

## Levene's Test

In statistics, Levene's test is an inferential statistic used to assess the equality of variances in different samples. Some common statistical procedures assume that variances of the populations from which different samples are drawn are equal. Levene's test assesses this assumption. It tests the null hypothesis that the population variances are equal (called homogeneity of variance). If the resulting p-value of Levene's test is less than some critical value (typically 0.05), the obtained differences in sample variances are unlikely to have occurred based on random sampling. Thus, the null hypothesis of equal variances is rejected and it is concluded that there is a difference between the variances in the population. Procedures which typically assume homogeneity of variance include analysis of variance and t-tests. **One advantage of Levene's test is that it does not require normality of the underlying data. Levene's test is often used before a comparison of means.** When Levene's test is significant, modified procedures are used that do not assume equality of variance. Levene's test may also test a meaningful question in its own right if a researcher is interested in knowing whether population group variances are different. This test employs a transformation of the original data values to difference values around each mean.

### Assumptions:

- Observed values  $X_{1,1}, X_{1,2}, X_{1,3}, \dots, X_{1,n1}$  are a random sample from
- Observed values  $X_{2,1}, X_{2,2}, X_{2,3}, \dots, X_{2,n2}$  are a random sample from
- Samples from the two samples are *independent*.

### Hypotheses:

For a two sided case:

$H_0: \sigma_1^2 = \sigma_2^2$  ... Meaning that there is no difference in variance between populations X1. & X2.

$H_1: \sigma_1^2 \neq \sigma_2^2$ ... Meaning that there is a difference in variance between populations X1 & X2

### Decision Rule:

If  $P < \alpha$ , then reject  $H_0$ , otherwise, accept  $H_0$

The p value can be ascertained from the output in R. The alpha value must be explicitly set, and is usually set to 0.05 or 0.01, depending on if the test is "minimally important" or "critically important," respectively.

The package that contains Levene's Test must be downloaded and installed before running the test.

- 1) Under the tab *packages*, select *install packages*
- 2) Select a CRAN mirror
- 3) Select package *car* and install it
- 4) **library(car)**
- 5) **?levene.test**

Example:  
> Loblolly

```
height age Seed
1 4.51 3 301
15 10.89 5 301
29 28.72 10 301
43 41.74 15 301
57 52.70 20 301
71 60.92 25 301
2 4.55 3 303
16 10.92 5 303
30 29.07 10 303
44 42.83 15 303
58 53.88 20 303
72 63.39 25 303
3 4.79 3 305
17 11.37 5 305
31 30.21 10 305
45 44.40 15 305
59 55.82 20 305
73 64.10 25 305
4 3.91 3 307
18 9.48 5 307
32 25.66 10 307
46 39.07 15 307
60 50.78 20 307
74 59.07 25 307
5 4.81 3 309
19 11.20 5 309
33 28.66 10 309
47 41.66 15 309
61 53.31 20 309
75 63.05 25 309
6 3.88 3 311
20 9.40 5 311
34 25.99 10 311
48 39.55 15 311
62 51.46 20 311
76 59.64 25 311
7 4.32 3 315
21 10.43 5 315
35 27.16 10 315
49 40.85 15 315
63 51.33 20 315
77 60.07 25 315
8 4.57 3 319
22 10.57 5 319
36 27.90 10 319
50 41.13 15 319
64 52.43 20 319
78 60.69 25 319
9 3.77 3 321
23 9.03 5 321
37 25.45 10 321
51 38.98 15 321
65 49.76 20 321
79 60.28 25 321
10 4.33 3 323
24 10.79 5 323
38 28.97 10 323
52 42.44 15 323
66 53.17 20 323
80 61.62 25 323
11 4.38 3 325
25 10.48 5 325
39 27.93 10 325
53 40.20 15 325
67 50.06 20 325
81 58.49 25 325
12 4.12 3 327
26 9.92 5 327
40 26.54 10 327
54 37.82 15 327
68 48.43 20 327
82 56.81 25 327
13 3.93 3 329
27 9.34 5 329
41 26.08 10 329
55 37.79 15 329
69 48.31 20 329
83 56.43 25 329
14 3.46 3 331
28 9.05 5 331
42 25.85 10 331
56 39.15 15 331
70 49.12 20 331
84 59.49 25 331
```

As an example, the dataset *Loblolly* (as presented) from R is used. The dataset uses samples from 84 Loblolly pine trees and lists their height, age and seed. The first column ranks each according to their height in increasing order.

To fit the format of the Levene Test, we must alter the data to fit what exactly we are trying to find, is there a variance between the age of the seed and the height it grows. To do this we categorize the ages of the seeds into *young* and *old*. Any seed  $\leq 10$  is deemed *young* and any seed  $> 10$  is deemed *old*. Our information now looks like this:

height	age	60.07	Old
4.51	Young	4.57	Young
10.89	Young	10.57	Young
28.72	Young	27.9	Young
41.74	Old	41.13	Old
52.7	Old	52.43	Old
60.92	Old	60.69	Old
4.55	Young	3.77	Young
10.92	Young	9.03	Young
29.07	Young	25.45	Young
42.83	Old	38.98	Old
53.88	Old	49.76	Old
63.39	Old	60.28	Old
4.79	Young	4.33	Young
11.37	Young	10.79	Young
30.21	Young	28.97	Young
44.4	Old	42.44	Old
55.82	Old	53.17	Old
64.1	Old	61.62	Old
3.91	Young	4.38	Young
9.48	Young	10.48	Young
25.66	Young	27.93	Young
39.07	Old	40.2	Old
50.78	Old	50.06	Old
59.07	Old	58.49	Old
4.81	Young	4.12	Young
11.2	Young	9.92	Young
28.66	Young	26.54	Young
41.66	Old	37.82	Old
53.31	Old	48.43	Old
63.05	Old	56.81	Old
3.88	Young	3.93	Young
9.4	Young	9.34	Young
25.99	Young	26.08	Young
39.55	Old	37.79	Old
51.46	Old	48.31	Old
59.64	Old	56.43	Old
4.32	Young	3.46	Young
10.43	Young	9.05	Young
27.16	Young	25.85	Young
40.85	Old	39.15	Old
51.33	Old	49.12	Old
		59.49	Old

It is now possible to run Levene's Test. To run the test in R, the program R must be able to read the data, so it is imperative to input the data into R.

```
> LT=read.table("c:/RData/LeveneTest.txt")  
> LT  
> attach(LT)
```

We can now run the test.

```
> leveneTest(height,age)  
Levene's Test for Homogeneity of Variance  
(center = median)  
  Df F value Pr(>F)  
group 1 0.3892 0.5345  
  82
```

We use the median as the center because it provides a more robust test. We have an alpha value of 0.05, and our p-value was found to be 0.5345. Based on decision rules, we can accept the Null Hypothesis that states that the population variances are equal.

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